

**Instructions:**

**Answer 3/4 out of the 6-8 questions.**

No extra credit will be given for more than ?? answers. If more than ?? questions are attempted, CLEARLY indicate which questions are to be graded, otherwise only the first ?? answers will be graded, and the rest ignored.

Show all calculation steps to ensure that partial credit is earned, even if the final answer is incorrect. In cases where the answer is obviously wrong, some credit will be given if you identify this as an improbable answer.

If you make any assumptions, clearly state these assumptions. If you run out of time briefly describe how you would answer the remaining questions, to receive partial credit

**Tillage Forces:**

$$D = F_o * [\sin(\zeta) + \mu' \cos(\zeta)] + C_\alpha A_0 \cos(\zeta) + kb \quad \text{Where:} \quad \mu = \tan(\Phi), \text{ and } \beta = (90 - \Phi)/2$$

$$D^* = W/Z + [CA_1 + B] / \{Z * [\sin(\beta) + \mu \cos(\beta)]\} + [C_\alpha A_0] / \{Z * [\sin(\zeta) + \mu' \cos(\zeta)]\}$$

$$Z = [\cos(\zeta) - \mu' \sin(\zeta)] / [\sin(\zeta) + \mu' \cos(\zeta)] + [\cos(\beta) - \mu \sin(\beta)] / [\sin(\beta) + \mu \cos(\beta)]$$

$$F_o = [D^* - C_\alpha A_0 \cos(\zeta)] / [\sin(\zeta) + \mu' \cos(\zeta)] \quad \gamma = \text{Bulk density (kg/m}^3\text{)}$$

$$A_1 = d * b / \{\sin(\beta)\} \quad b = \text{tool width (m)}$$

$$A_0 = b * L_o \quad d = \text{depth (m)}$$

$$W = g * \gamma * b * d^\ddagger * [L_o + (L_1 + L_2) / 2] \quad d^\ddagger = d * [\sin(\zeta + \beta)] / \{\sin(\beta)\}$$

$$B = \gamma * d * b * (V_o)^2 * [\sin(\zeta)] / [\sin(\zeta + \beta)] \quad L_1 = d * [\cos(\zeta + \beta)] / \{\sin(\beta)\}$$

$$g = \text{gravity} \quad L_2 = d^\ddagger * \tan(\zeta)$$

**Orifice Flow:**

$$Q = -.0342 + 770 A_n * (g * D_e)^{(0.5)} \quad \text{Where: } D_e = D - k * d \text{ (circular)}$$

$$a' = a - k * d, \quad b' = b - k * d, \quad D_e = 0.5 * a' * b' / (a' + b') \text{ (rectangular)}$$

**Rotary Spreader**

$$\{ (C_1 + f) \exp[C_2 * (C_1 - f) * \theta] + (C_1 - f) \exp[-C_2 * (C_1 + f) * \theta] \} / \{ 2 * C_1 \}$$

$$= \{ r_o - (C_3 * g) / (C_4 * \omega * \omega) \} / \{ C_5 r_i - (C_3 * g) / (C_4 * \omega * \omega) \}$$

$$V_r = \omega / (2 * C_1) * \{ C_5 r_i - (f * g) / (\omega * \omega) \} * \{ \exp[C_2 * (C_1 - f) * \theta] - \exp[-C_2 * (C_1 + f) * \theta] \}$$

$$V_{hr} = \{ (V_r * \cos(\alpha) * \cos(\gamma))^2 + (r_o * \omega + V_r * \cos(\alpha) * \sin(\gamma))^2 \}^{0.5}$$

$$\beta = \text{atan} \{ [ V_r * \cos(\alpha) * \cos(\gamma) ] / [ r_o * \omega + V_r * \cos(\alpha) * \sin(\gamma) ] \}$$

$$V_v = V_r * \sin(\alpha)$$

Where :

$$C_1 = (f * f + C_4 / C_2)^{0.5} \quad C_2 = \cos(\alpha) \quad C_3 = \sin(\alpha) + f * \cos(\alpha)$$

$$C_4 = \cos(\alpha) - f * \sin(\alpha) \quad C_5 = \cos(\zeta) - f * \sin(\zeta) \quad \gamma = \text{atan} [ r_i * \tan(\zeta) / (r_o - r_i) ]$$